### Network-based interpretation of sequence variants

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#### **Computational Network Biology**

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#### **RECAP of problems in network biology**

#### **Biological problem**

- Mapping regulatory network structure
- Dynamics and context specificity of networks
- Understanding design principles of biological networks
- Interpretation of sequence variants/perturbations
- Identification of important genes
- Integrating different types of molecular genomic data
- Smoothing noisy matrices

#### **Computational approaches**

- Probabilistic graphical models
- Graph structure learning
- Multiple network learning
- Topological properties of graphs
- Graph clustering
- Graph alignment
- Diffusion on graphs

#### Graph diffusion based methods

- Aim to use the graph structure to define similarity between nodes on the graph
- The similarity function is also sometimes referred to as a "kernel"
  - Random walk kernel, Diffusion kernel
- Many applications
  - Gene prioritization
  - Smoothing of count matrices
  - Interpreting variants on networks

#### **Overview of network-based gene** prioritization



This is for GeneWanderer, but other approaches are similar.

#### Motivation of using global distance



- Global similarity is more sensitive and different for each of the above cases
- In contrast, local shortest-path similarity is the same for all pairs
- Direct interactions will never select y as a candidate

# RECAP of graph diffusion based gene prioritization

- We discussed the GeneWanderer method
- Focus on global rather than local graph distances
- Global distances can be obtained using random walks or a diffusion kernel
- Global distances were able to rank known disease genes much better than shortest path based methods
- Network-based prioritization can be used when we have a small number of known genes to start with

#### **Perturbations in networks**

- Understanding genetic perturbations are important in biology
- Genetic perturbations are useful to identify the function of genes
  - What happens if knock gene A down?
    - Measure some morphological phenotype like growth rate or cell size
    - Measure global expression signatures
- Perturbations can be artificial or natural
  - Artificial perturbations
    - Deletion strains
  - Natural perturbations
    - Single nucleotide polymorphisms
    - Natural genetic variation
- Perturbations in a network can affect
  - Nodes or edges
  - Edge perturbations
    - Mutations on binding sites

#### Types of algorithms used to examine perturbations in networks

- Graph diffusion followed by subnetwork finding methods
   HOTNET
- Probabilistic graphical model-based methods
  - Factor graphs
  - Nested Effect Models (NEMs)
- Information flow-based methods (also widely used for integrating different types of data)
  - Prize collecting steiner tree
  - Min cost max flow

#### Identification of subnetworks perturbed in diseases



Cho D-Y, Kim Y-A, Przytycka TM (2012) Chapter 5: Network Biology Approach to Complex Diseases. PLoS Comput Biol 8(12): e1002820. doi:10.1371/journal.pcbi.1002820 http://www.ploscompbiol.org/article/info:doi/10.1371/journal.pcbi.1002820

### **Motivation of HOTNET**

- Somatic mutations play a major role in cancer
- Mutation profiles of cancers is very heterogeneous
  - Tumors harbor on average approximately 80 somatic mutations, but two tumors rarely have the same complement of mutations
- Thousands of genes can be mutated in cancer
  - This makes it difficult to identify "driver" mutations vs "passenger" mutations
  - Mutations at the pathway level (group of genes) is likely responsible for a particular type of cancer
- Can we identify subnetworks (representing new pathways) that are significantly mutated?

F. Vandin, E. Upfal, and B. J. Raphael, "Algorithms for detecting significantly mutated pathways in cancer." *Journal of computational biology* 2011

### **HOTNET problem setup**

- Given
  - A network of protein-protein interactions
  - A set of patient tumor mutation profiles
- Do
  - Find "significantly" mutated subgraphs
    - A subgraph that best connects these genetic alterations
    - Best means a subgraph that includes as many tumour samples with as few genes
- How?
  - Find the global influence of mutations on a particular gene
  - Search for a subnetwork in this global influence graph that is significantly mutated

#### **HOTNET's approach vs ActiveSubgraphs**

- HOTNET aims to find a subnetwork that has significantly many more mutations than random subnetworks
- This bears some resemblance to the ActiveSubgraph approach where we were trying to find subnetworks significantly up or down-regulated
- The key differences in HOTNET is that
  - we do not have (gene expression) measurement of mutations for all genes
  - only a small number of genes maybe mutated

### Key steps of HOTNET algorithm

- Build an influence graph which specifies the influence of one node over another
  - Graph diffusion
  - Builds a network with the tested genes as well as their neighborhood
- Find significantly mutated subnetworks (two ways)
  - include genes mutated in a lot of samples
  - Enhanced influence model where the influence edges are weighted by the number of mutations
- Test for the significance of the number of subnetworks of a particular size

### **Diffusion kernel used in HOTNET**

- HOTNET uses a specific type of kernel called the heat diffusion kernel
- L=D-A denotes the graph Laplacian, where A is the adjacency matrix and D is the degree matrix
- Let  $\gamma$  denote the constant rate at which heat is lost at any node
  - E.g. this could be proportional to the mean degree
- $L_{\gamma}$  is  $L+\gamma I$
- Let *s* be a source node
- The influence of *s* on all *n* nodes at time *t* is denoted as  $\mathbf{f}^{s}(t) = [f_{1}^{s}(t), \cdots, f_{n}^{s}(t)]$

Influence of s on node 1

#### **Diffusion kernel used in HOTNET**

• Rate at which diffusion occurs from a source node on the graph is given by  $d\mathbf{f}^s(t) = \mathbf{f}^s(t) + \mathbf{h}^s(t)$ 

$$\frac{d\mathbf{r}(t)}{dt} = -L_{\gamma}\mathbf{f}^{s}(t) + \mathbf{b}^{s}$$

- where **b**<sup>s</sup> be a unit vector which is 1 for node s and 0 otherwise
- The influence on all nodes at steady-state is given by

$$\mathbf{f}^s = L_{\gamma}^{-1} \mathbf{b}^s$$

• This diffusion process is very similar to what we had in the Diffusion kernel we used for ranking genes

### Graph diffusion to downplay hub intermediate nodes



Mutations in a linear chain are more "interesting" than in a star graph

## Computing the influence between vertex pairs

- Assume we have two vertices *u* and *v*
- Let i(u,v) be the influence from u to v
- w(u,v) is the influence between u and v and is min[i(u,v),i(v,u)]
- The influence graph is thus an *n* X *n* symmetric weighted graph, where *n* is the number of tested genes
- Further prune by removing edges with weight  $w(u,v) < \delta$

### Key steps of HOTNET algorithm

- Build an influence graph which specifies the influence of one node over another
  - Graph diffusion
  - Builds a network with the tested genes as well as their neighborhood
- Find significantly mutated subnetworks (two ways)
  - Set cover to include genes mutated in many samples
  - Enhanced influence model where the influence edges are weighted by the number of mutations
- Test for the significance of the number of subnetworks of a particular size

#### HOTNET's maximal connected cover approach

- Given
  - A weighted influence network G=(V,E)
  - T be a subset of V, comprising genes with a mutation
  - $P_{v_i}$ : the set of samples with mutation in gene  $v_i$
- Do:
  - Find a subnetwork over gene subset C that covers a maximal number of mutated samples
  - Formally, we want to find a C={v<sub>1</sub>,...v<sub>k</sub>} such the following is maximized:

$$\bigcup_{j=1}^k P_{v_j} |$$

#### Heuristic algorithm to find a maximal connected cover

- Finding the maximal connected cover set is computationally difficult
- A heuristic algorithm is used
- Add a vertex v such it is connected to the current vertex set via a node u, and maximizes the ratio of the number of new samples covered to the number of nodes between u and v

#### Heuristic algorithm to find a maximal connected cover

#### **Combinatorial Algorithm**

**Input:** Influence graph  $G_I$  and parameters  $\delta$  and k **Output:** Connected subgraph  $\mathcal{C}$  of  $G_{I}(\delta)$  with k vertices Construct  $G_I(\delta)$  by removing from  $G_I$  all edges with weight  $< \delta$ ; 1 **2**  $\mathcal{C} \leftarrow \emptyset$ : 3 for each node  $v \in V$  do Exploration 4  $C_v \leftarrow \{v\};$ 5 for each  $u \in V \setminus \{v\}$  do  $p_v(u) \leftarrow$  shortest path from v to u in  $G_I(\delta)$ ; while  $|\mathcal{C}_{v}| < k$  do 6  $//\ell_{v}(u) = set of nodes in p_{v}(u); P_{v}(u) = elements of I covered by$  $\ell_{v}(u)$ ;  $P_{C_{v}} = elements$  covered by  $C_{v}$ ;  $P_{C} = elements$  covered by C $u \leftarrow \arg\max_{u \in V \setminus \mathcal{C}_{\nu}: |\ell_{\nu}(u) \cup \mathcal{C}_{\nu}| \leq k} \left\{ \frac{|P_{\nu}(u) \setminus P_{\mathcal{C}_{\nu}}|}{|\ell_{\nu}(u) \setminus \mathcal{C}_{\nu}|} \right\}; \text{ Keep adding a neighbor that has the maximal coverage with }$ 7 8 if  $|P_{\mathcal{C}_{\nu}}| > |P_{\mathcal{C}}|$  then  $\mathcal{C} \leftarrow \mathcal{C}_{\nu}$ : fewest additional vertices 9 **10 return** C;

### **Enhanced influence model**

- The enhanced influence model was a more computationally efficient approach
- Enhance the influence measure between genes by the number of mutations observed in each of these genes
- Specifically, let  $v_i$  and  $v_k$  be two genes with a mutation

$$h(v_j, v_k) = w(v_j, v_k) \times max\{|S_j|, |S_k|\}$$
  
Enhanced influence Set of samples with mutation in  $v_i$ 

- Remove edges with influence  $<\!\delta$
- Decompose the associated enhanced influence graph into connected components

# Statistical analysis for determining significance of subnetworks

Null distribution of subnetworks

- Assign mutations uniformly at random
- Shuffle gene labels in mutation data (preserve mutation frequencies)
- Assess significance of the total number of subnetworks with *s* or more genes

#### **Application of HOTNET to cancer dataset**

- 453 mutations in 601 genes in 91 Glioblastoma (GBM) samples
- 1,013 mutations in 623 genes in 189 samples of lung adenocarcinoma
- Protein-protein interaction network with 18796 genes and 37,107 edges

#### HOTNET recovers pathways relevant to cancer

Dataset	k	Samples	p-value		Pathway enrichment p-value		
			$H_0^{\text{sample}}$	$H_0^{\text{gene}}$	All	RTK/RAS/PI(3)K	p53
GBM	10	67	$< 10^{-10}$	$4 \times 10^{-3}$	$3 \times 10^{-4}$	$8 \times 10^{-4}$	0.19
	20	78	$< 10^{-10}$	$< 10^{-3}$	$10^{-5}$	$8 \times 10^{-5}$	0.05
Lung	10	140	$< 10^{-10}$	0.02	$8 \times 10^{-6}$	/	
	20	151	$< 10^{-10}$	0.03	$3 \times 10^{-3}$	/	

 TABLE 1.
 RESULTS OF THE COMBINATORIAL MODEL

k is the number of genes in the subnetwork. Samples is the number of samples in which the subnetwork is mutated. *p-value* is the probability of observing a connected subgraph of size k mutated in a number of samples  $\geq$  samples under the random model  $H_0^{\text{sample}}$  or  $H_0^{\text{gene}}$ . enrichment *p-value* is the *p*-value of the hypergeometric test for overlap between genes in the identified subgraph and genes reported significant pathways in TCGA (2008) or Ding et al. (2008). For GBM, enrichment *p-value* is the *p*-value of the hypergeometric test for RTK/RAS/PI(3)K and p53 pathways.

# Application of HOTNET of pan-cancer mutation analysis

- More recently, an updated version of HOTNET (HOTNET2) was applied to mutation profiles of samples from 12 different cancers
- Dataset description
  - After data pre-processing there were 3,110 samples with mutations in 11,565 genes
  - Genes mutation frequency varied a lot: 1-1,291 samples

M. D. M. Leiserson, F. Vandin, H.-T. Wu, J. R. Dobson, J. V. Eldridge, J. L. Thomas, A. Papoutsaki, Y. Kim, B. Niu, M. McLellan, M. S. Lawrence, A. Gonzalez-Perez, D. Tamborero, Y. Cheng, G. A. Ryslik, N. Lopez-Bigas, G. Getz, L. Ding, and B. J. Raphael, "Pan-cancer network analysis identifies combinations of rare somatic mutations across pathways and protein complexes," *Nature Genetics*, vol. 47, no. 2, pp. 106-114, Dec. 2014. [Online].

#### **HOTNET versus HOTNET2 kernel**

Hotnet kernel

Rate of diffusing out

$$(L + \gamma I)^{-1}$$

• Hotnet2 kernel

Fraction of heat that stays on a node

$$\beta (I - (1 - \beta)W)^{-1}$$

The Hotnet2 kernel was specifically designed to further avoid "star" subnetworks.

#### HOTNET2 for pan-cancer mutation analysis

b

#### a



Very hot genes

Leiserson et al . 2014, Nature Genetics

#### HOTNET2 for pan-cancer mutation analysis



HOTNET2 subnetworks include genes with a wide range of mutation frequency

#### **Overview of HOTNET2 results**



#### SWI/SNF complex pathways identified by Number of samples HOTNET2



Sixth most mutated Hotnet2 subnetwork.

#### **HOTNET** summary

- An algorithm to find significantly mutated subnetworks
- Based on creating an "influence graph", followed by identification of "interesting" subnetworks
- Non-local, less sensitive to network hubs
- Note: the subgraph detection component could be also addressed using module detection algorithms
- Post diffusion the graph could be used also for network-based stratification

# Network-based stratification of patient samples

Input: Patient tumour mutation profiles, skeleton network

Output: Patient groups

**How**: (1) Smooth mutation profile using network smoothing; (2) Use Non-negative Matrix Factorization to cluster samples



Hofree et al. 2013, Nature methods

### Network-based stratification of patient tumor samples

**Uterine cancer** 

NBS subtypes associated with different histological types

**Ovarian cancer** 

NBS subtypes associated with survival



Hofree et al., Nature Methods 2013

#### Types of algorithms used to examine perturbations in networks

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  - Min cost max flow
  - Prize collecting steiner tree

#### Probabilistic graphical models for interpreting network perturbations

- "Inference of Patient-Specific Pathway Activities from Multi-Dimensional Cancer Genomics Data Using PARADIGM. Bioinformatics" <u>https://academic.oup.com/bioinformatics/article/2</u> <u>6/12/i237/282591</u>
- C.-H. H. Yeang, T. Ideker, and T. Jaakkola, "Physical network models." Journal of computational biology : a journal of computational molecular cell biology, vol. 11, no. 2-3, pp. 243-262, Mar. 2004.
- F. Markowetz, D. Kostka, O. G. Troyanskaya, and R. Spang, "Nested effects models for high-dimensional phenotyping screens," *Bioinformatics*, vol. 23, no. 13, pp. i305-312, Jul. 2007.
- C. J. Vaske, C. House, T. Luu, B. Frank, C.-H. H. Yeang, N. H. Lee, and J. M. Stuart, "A factor graph nested effects model to identify networks from genetic perturbations." *PLoS computational biology*, vol. 5, no. 1, pp. e1 000 274+, Jan. 2009.
# PARADIGM for detecting pathway activities



## Factor graphs

- A type of graphical model
- A bi-partite graph with variable nodes and factor nodes
- Edges connect variables to potentials that the variables are arguments of
- Represents a global function as product of smaller local functions
- Perhaps the most general graphical model
  - Bayesian networks and Markov networks have factor graph representations

### Example factor graph



Fig. 1. A factor graph for the product  $f_A(x_1)f_B(x_2)f_C(x_1, x_2, x_3)$  $\cdot f_D(x_3, x_4)f_E(x_3, x_5)$ .

From Kschischang, Frey, Loeliger 2001

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# Motivation of nested effect models

- Perturbation of genes followed by high-throughput profiling of different phenotypes can be used to characterize functions of genes
- However, most genes do not function independently but interact in a network to drive a particular function
- Phenotypic measurements (e.g. mRNA levels) are indirect measurements of the underlying network structure
  - Includes direct and indirect effects
- Given perturbation data from multiple genes, can we more systematically identify the functions of these genes and how they interact at a pathway level?

### **Problem overview**

- Given
  - global measurements of gene expression after single gene deletions of multiple genes
- Do
  - Infer interactions between genes with deletions to enable further characterization of these genes
- Nested Effect Models are probabilistic model-based approaches to solve this problem

### **Nested Effect Models**



Fig. 1. An introduction to Nested Effects Models. Plot (a) shows a toy dataset consisting of phenotypic profiles for eight perturbed genes  $(A, \ldots, H)$ . Each profile is binary with *black* coding for an observed effect and *white* for an effect not observed. The eight profiles are hierarchically clustered, showing that they fall into four pairs of genes with almost identical phenotypic profiles: (A, B), (C, D), (E, F) and (G, H), as shown in plot (b). An important feature of the data missed by clustering is the subset structure visible between the profiles in the data set: the effects observed when perturbing genes A or B are a superset to the effects observed for all other genes. The effects of perturbing G or H are a subset to all other genes' effects. The pairs (C, D) and (E, F) have different but overlapping effect sets. The directed acyclic graph (DAG) shown in plot (c) represents these subset relations, which are shown in plot (d). Compared to the clustering result in plot (b) the NEM additionally elucidates relationships between the clusters and thus describes the dominant features of the data set better.

Markowetz et al, 2007

### **Nested Effect Models Key properties**

- A generalization of similarity based clustering
- Orders the clusters according to subset relationships
  - A gene A is upstream of another gene B if B's effects are a subset of A's effects
- Build a hierarchy of all perturbed genes by constructing from smaller sub-models of pairs and triplets of genes

#### Subset relationships to order genes



A complete model. The left part of the figure shows a complete model M'<sub>xyz</sub> consisting of a transitively closed graph between genes and assignments of genes to specific effects (the dashed arrows). Given the complete model, we can formulate a prediction of what effects to expect: perturbing x should cause all effects, while perturbing y should only cause E3–E6, and perturbing z only E5 and E6 (middle plot). In reality, our observations will be noisy: there can be false positive (FP) and false negative (FN) effect observations (right plot).

### Probabilistic graphical models for interpreting network perturbations

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#### Key properties of Factor Graph-NEMs (FG-NEMs)

- NEMs assume the genes that are perturbed interact in a binary manner
- But many interactions have sign
  - inhibitory or stimulating action
- FG-NEMs capture a broader set of interactions among the perturbed genes
- Formulation based on a Factor Graph
  - Provide an efficient search over the space of NEMs

# Notation

- S-genes: Set of genes that have been deleted individually
- E-genes: Set of effector genes that are measured
- $\Theta$ : The attachment of an effector gene to the S-gene network
- $\Phi$ : The interaction matrix of S-genes
- X: The phenotypic profile, each column gives the difference in expression in a knockout compared to wild type
  - Rows: E-genes
  - Columns: S-genes
- Y: Hidden effect matrix, each entry is {-1, 0, +1} which specifies whether an S-gene affects the E-gene

#### An example of 4 S-genes and 13 E-gens



# S-gene interaction modes and their expression signatures



Expected trend in E-genes for specific interaction modes

Inconsistent with expectation

### Factor graph representation of NEMs



# **Probabilistic model for NEMs**

- Goal is to find a network, Φ and Θ that best fit the observed data (X)
- This is an inference problem
- Use a Maximum a posterior (MAP) approach

$$J(X) = \max_{\phi,\theta} P(\phi, \theta | X)$$
$$J(X) = \max_{\phi,\theta} \sum_{Y} P(\phi, \theta, Y | X)$$

Makes use pairwise potentials to make the computation tractable

X is a noisy measurement of Y. Y is the quantity we need to sum over

# Inference on the factor graph

- Find most likely configurations for  $\phi_{A,B}$
- Use a message passing algorithm (standard for factor graphs)
- Called the Max-Product algorithm
- Message passing happens in two steps
  - Messages are passed from observations  $X_{eA}$  to the  $\phi_{A,B}$
  - Messages are passed between the interaction and transitivity factors until convergence

# Does FG-NEM capture activating and inhibitory relationships?

FG-NEM: capture inhibitory and activating relationships uFG-NEM: capture only unsigned interactions FG-NEM AVT: FG-NEM run on absolute value data Solid lines: structure recovery Dashed lines: sign recovery



# Does FG-NEM expand pathways better than the baseline approach



### Pathway expansion

- Attach new E-genes to S-gene network
- An attached gene *e* to S-gene *s* asserts that *e* is directly downstream of *s*
- All E-genes attached to the S-gene network are called frontier genes
- An E-gene's connectivity is examined based on the Loglikelihood Attachment Ratio

$$LAR(e) = \log\left(\frac{\max_{i \neq 0} P(X_e | \Phi, \theta_e = i)}{P(X_e | \Phi, \theta_e = 0)}\right)$$
 One of the S genes

# FG-NEM based pathway expansion in yeast



Template matching: rank E genes based on similarity in expression to an "idealized template"

# FG-NEM infers a more accurate network than the unsigned version in yeast



- FG-NEM and uFG-NEM networks inferred in the ion-homeostasis pathway
- FG-NEM inferred more genes associated with ion homeostatis compared to uFG-NEM

#### **FG-NEM** application to colon cancer



# Summary

- FG-NEMs: A general approach to infer an ordering of genes from knock-down phenotypes
- Strengths
  - FG-NEMs could be used in an iterative computationalexperimental framework
  - Handles signed interactions between S-genes
- Weaknesses
  - Computational complexity of the inference procedure might be high
    - Required independence among E-genes
    - Model pairs of S-genes at a time

### **Overall conclusion**

- Networks are powerful models for interpreting sequence variants or genetic perturbations as such
- We have see two classes of methods
  - Extract a weighted graph based on the influence of a mutation on one node to another
  - Probabilistic approaches
- A systematic comparison of these two classes of methods has not been done so far.